

An inner boundary condition for solar wind models based on coronal density

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ABSTRACT

Accurate forecasting of the solar wind has grown in importance as society becomes increasingly dependent on technology that is susceptible to space weather events. This work describes an inner boundary condition for ambient solar wind models based on tomography maps of the coronal plasma density gained from coronagraph observations, providing a novel alternative to magnetic extrapolations. The tomographical density maps provide a direct constraint of the coronal structure at heliocentric distances of 4 to $8R_{\odot}$, thus avoiding the need to model the complex non-radial lower corona. An empirical inverse relationship converts densities to solar wind velocities which are used as an inner boundary condition by the Heliospheric Upwind Extrapolation (HUXt) model to give ambient solar wind velocity at Earth. The dynamic time warping (DTW) algorithm is used to quantify the agreement between tomography/HUXt output and *in situ* data. An exhaustive search method is then used to adjust the lower boundary velocity range in order to optimize the model. Early results show up to a 32% decrease in mean absolute error between the modelled and observed solar wind velocities compared to that of the coupled MAS/HUXt model. The use of density maps gained from tomography as an inner boundary constraint is thus a valid alternative to coronal magnetic models, and offers a significant advancement in the field given the availability of routine space-based coronagraph observations.

Subject headings: Sun: corona—sun: CMEs—sun: solar wind

1. Introduction

Rapid changes in solar wind conditions have a direct impact on Earth's magnetosphere (e.g., Meziane et al. 2014), ionosphere (e.g., Milan et al. 2007), and both ground-based and space-based technology (e.g., Imken et al. 2018; Baker et al. 2004; Doherty et al. 2004). Estimates of economic impact of space weather on European power grids alone range from €10s-100s billion (e.g., Eastwood

et al. 2018). Risk can be mitigated considerably by early warnings of impending space weather, currently undertaken by organisations such as the Meteorological Office in the UK. We believe that improvements in space weather forecasting depend primarily on three related categories: (1) Better observations of the Sun, corona, and solar wind; (2) Greater understanding of the physical processes operating in the corona and solar wind; (3) Improvements in data analysis and forecasting methods. This work presents a novel boundary condition to solar wind models based on tomography maps created from coronagraph observations of the solar atmosphere, thus an advancement that belongs to the third category, and can contribute to the second.

The use of tomography maps as an inner boundary condition to a solar wind model, combined with an ensemble approach, plays a key role in the Coronal Tomography (CorTom) module to the Space Weather Empirical Ensemble Package (SWEEP) project. SWEEP is funded by the UK government’s Space Weather Instrumentation, Measurement, Modelling, and Risk (SWIMMR) scheme and will provide an operational space weather prediction package to the UK Meteorological Office by 2023. The SWEEP package operates a robust, complimentary framework of multiple models using different boundary conditions including the tomography described in this paper, and both simple and more sophisticated magnetic models (Yeates et al. 2018; Weinzierl et al. 2016; Gonzi et al. 2021).

Approaches to space weather forecasting can be broadly placed in two groups: simulations that use observations of the Sun’s photosphere to drive a model of the solar wind (e.g., Wang-Sheeley-Arge (WSA)/ENLIL: Arge and Pizzo 2000; Wang and Sheeley 1990) and a persistence based approach which extrapolates the future behavior of the solar wind based on its past behavior over various timescales (Owens 2018). A persistence based approach assumes that the ambient solar wind does not evolve drastically over a solar rotation. This is shown in observational data by a weak recurrence in geomagnetic activity and solar wind conditions (Diego et al. 2010) over a ~ 27 day period. Hence a persistence approach can provide a baseline for comparison of solar wind forecasting models (Owens et al. 2013). The heliospheric simulations are primarily based on remote solar observations and depend on photospheric magnetic field observations to build a model of the corona (e.g, MAS: Linker et al. 1999; Riley et al. 2012, AWSom: der Holst et al. 2014, etc.). It is the modelled conditions of the outer corona that forms the inner boundary for heliospheric solar wind models (e.g, ENLIL: Odstrcil 2003, EUHFORIA: Pomoell, J. and Poedts, S. 2018, HUXt: Owens et al. 2020).

The Magnetohydrodynamic Algorithm outside a Sphere (MAS) coronal model uses photospheric magnetic field observational data in order to gain the magnetic field configuration at the solar wind base (Linker et al. 1999; Riley et al. 2012). MAS derives an inner boundary condition at $30R_{\odot}$ that can be used in solar wind heliospheric models to predict solar wind conditions at 1AU (Owens and Riley 2017). In this work, the MAS inner boundary condition is used to benchmark the results of the tomography derived inner boundary condition. MAS adopts a simplified coronal ‘polytropic’ model which assumes the thermal pressure is greater or equal to the magnetic pressure at distances closer to the sun (i.e., $\beta \geq 1$). This is used to empirically convert the pressure and

density, which are gained via simplified physical laws, into a solar wind solution (Parker et al. 1964). Magnetohydrodynamic (MHD) equations are used and integrated forward in time until the solar wind parameters reach a steady-state and give a full three dimensional state of the solar wind at heights greater than the solar wind Alfvén point (Linker et al. 1999; Riley et al. 2012). MHD heliospheric models use this information at $30R_{\odot}$ as inner boundary conditions in order to propagate the solar wind conditions to 1AU (Odstrcil 2003; Owens et al. 2020; Riley and Lionello 2011). Three-dimensional MHD models offer a comprehensive physical model of the solar wind at large scales, but are computationally expensive.

Riley and Lionello (2011) proposed that the magnetic, gravitational, and pressure gradient forces of the solar wind plasma can be neglected at distances greater than $30R_{\odot}$, and that a purely radial flow of the ambient solar wind plasma can be assumed, thus vastly reducing the complexity of the MHD equations. Heliospheric models that use this reduced physical approach have a greatly increased computational efficiency at the expense of reduced physics whilst still yielding results comparable to full 3D MHD models (e.g., Owens et al. 2020). Owens et al. (2020) has adapted this reduced physical model for the time domain, namely the ‘Time-dependent Heliospheric Upwind Extrapolation’ (HUXt) model. The model complexity is reduced further when limited to only radial components of the equatorial plane, allowing the model to run on a standard desktop computer in seconds, even with a moderate angular ($\sim 2.8^{\circ}$), radial ($1.5R_{\odot}$), and time (~ 4 hour) resolution.

Whilst space weather forecasting has developed enormously over the past few decades, there is still large room for further improvement. One of the main constraints on the accuracy of space weather forecasting is the lack of adequate observational data that constrains direct empirical models between the photosphere and Earth. According to the concluding sentences of MacNeice et al. (2018): ‘the pace of [physical model] development has outstripped the pace of improvements in the quality of the input data which they consume, and until this is remedied, these models will not achieve their full forecasting potential’. This statement is a strong argument for new instruments and missions that are focused on operational space weather to provide higher quality data. It is also an argument for full exploitation of current resources: new or improved constraints on coronal structure and density at the coronal-heliosphere boundary are therefore important. Recent efforts are focused on improving the diagnostics from photospheric observations through advanced magnetic modelling, or to use alternative observations such as radio scintillation (Gonzi et al. 2021). Our efforts are focused on using coronagraph observations through coronal rotation tomography to provide a direct constraint on solar wind models. A less direct approach developed by Poirier et al. (2021) is to use coronagraph observations to constrain magnetic models without resolving the line of sight (LOS).

There are ample, routine, observations made of the coronal-heliospheric boundary region by space-based coronagraphs (e.g., LASCO Brueckner et al. 1995, COR2: Howard et al. 2008). These are largely neglected in the context of ambient solar wind modelling due mainly to the LOS problem: given the complex spatial distribution of high- and low-density streams along the LOS it is impossible, from a single observation, to estimate this distribution. Coronal rotational tomography

techniques aim to find a distribution of electron density in a 3D corona which best satisfy a set of coronagraphic polarized brightness (pB) observations made over half a solar rotation (half a rotation since both east and west limbs are observed), subject to some reasonable assumptions such as the smoothness of the reconstruction, thus helping to rectify the LOS problem. A comprehensive review is given by Aschwanden (2011). An iterative regularised least-square fitting method was presented by Frazin (2000), and developed and applied to other cases (e.g., Butala et al. 2005). A similar method has been applied to very low heights in the corona (Kramar et al. 2014), and expanded to include a time-dependency (e.g., Vibert et al. 2016). A novel method for creating qualitative maps of the distribution of coronal structure was introduced by Morgan et al. (2009), resulting in a comprehensive study of coronal structure over a solar cycle (Morgan and Habbal 2010a) and measurements of coronal rotation rates (Morgan 2011). Machine learning approaches are currently being developed (Jang et al. 2021). A new quantitative method based on spherical harmonics is presented by Morgan (2019), utilising the calibration and processing methods of Morgan (2015). Further refinements to the method, and initial results, are presented in Morgan and Cook (2020), and a study of coronal rotation rates based on the tomography is made by Edwards et al. (2022). The method is based on a spherical harmonic model of the coronal electron density, and gives reconstructions at distances of 4 to $10R_{\odot}$. At these heights and above, the corona can be assumed to flow radially outward. The tomography results when compared at different heights, confirm this radial structure (Morgan and Cook 2020). A desirable goal over the next decade would be an unified approach, where solar wind models are driven by coronal models based on as many empirical constraints as possible, including magnetic field extrapolations, coronal density estimations, and any other routine empirical constraints such as outflow velocity estimations. A crucial advancement would be the inclusion of a time-dependent inner boundary condition based on time-dependent magnetic models (e.g. Yeates et al. 2008; Weinzierl et al. 2016), and time-dependent tomography (e.g. Morgan 2021; Vibert et al. 2016). Morgan (2021) state that the time-dependent method requires further development for routine use, thus our current work uses the static tomography method of Morgan and Cook (2020).

The aim of this work is to improve the accuracy of predictions of the ambient solar wind velocity at Earth, and to investigate the relationship between coronal electron density and solar wind velocity at a distance of $8R_{\odot}$. Although iterative tomography methods have been coupled with MHD models to forecast space weather before (e.g., HELTOMO Jackson et al. 2020), these models and studies are primarily focused on Coronal Mass Ejections (CME) (Jackson et al. 2010) and use an iterative integrated kinematic model in order to predict ambient solar wind conditions (Jackson et al. 2013). Such heliospheric models incorporate CME models such as the cone model (Odstrcil et al. 2004), which use observational constraints on CME characteristics in order to model CME propagation throughout the heliosphere. CMEs are not considered further in this work, although our method and results are relevant to CME propagation and arrival time predictions.

This work proposes to use the tomography results as a new inner boundary condition for heliospheric solar wind models (HUXt), describes an initial implementation, and presents initial

results compared to boundary conditions based on MAS as a proof of concept. The methodology used in this study as well as the simple empirical relationship used to derive solar wind velocity from density at a distance of $8R_{\odot}$, are described in section 2. The iterative method used to improve the model’s match to *in situ* data through adjustment of input parameters is given in section 3.1. MAS inner boundary conditions, when coupled with 3D MHD heliospheric models, have produced results that compare well with *in situ* (OMNI) bulk solar wind velocity data (e.g., Owens and Riley 2017). The optimised model output is compared to results gained by using MAS-derived inner boundary condition and *in situ* data obtained via Operating Missions as Nodes on the Internet (OMNI) satellite network in section 3.2. The tomography-based model is then applied to dates at different stages of solar cycle 24 in section 3.3. Section 3.4 explores the operational feasibility of the tomography inner boundary condition by adopting a persistence-based approach. Section 4 presents an implementation of an ensemble model that demonstrates how uncertainties can be quantified by the system. Conclusions are given in section 5.

2. Method

This section gives a brief overview of the tomography method (section 2.1), outlines the method to generate the inner boundary velocity condition from the tomography density maps (section 2.2), gives an overview of the the heliospheric solar wind model (section 2.3), and an overview of the Dynamic Time Warping (DTW) algorithm and how this will be exploited in the context of this study (section 2.4).

2.1. Tomography Maps of the Solar Corona

The COR2 coronagraphs are part of the Sun Earth Connection Coronal and Heliospheric Investigation (SECCHI: Howard et al. 2008) suite of instruments aboard the twin Solar Terrestrial Relations Observatory (STEREO A & B: Kaiser 2005). Density maps are calculated from COR2A data in 3 main steps:

- Calibration is applied to COR2 polarized brightness (pB) observations over a period of half a Carrington rotation (± 1 week from the required date) using the procedures of Morgan (2015). The processing includes a method to reduce the signal from coronal mass ejections (CMEs) (Morgan et al. 2012). Following calibration, the data is remapped in solar polar co-ordinates, and an annular slice at the required distance from sun center extracted over several hundred observations taken over the time period. Figure 1a shows an example of data used as input for the tomography. For this example, the central date is 2018/11/11 12:00, the data spans a period from 2018/11/04 00:00 to 2018/11/17 23:08, and the distance chosen is $8R_{\odot}$. This date range corresponds approximately to the mid-date of Carrington rotation (CR) 2210.

- Tomography is applied to the data using the regularized spherical-harmonic optimization approach of Morgan (2019). The method is based on a spherical harmonic distribution of density at the height of reconstruction, with a $r^{-2.2}$ decrease in density above this inner height, thus a purely radial density structure is prescribed. Line-of-sight integrations are made of the spherical-harmonic based densities, thus a set of brightnesses are gained, one for each order, with the lines-of-sight corresponding to the COR2A observations. The problem is then reduced to finding the coefficients of each order based on a regularised least-squares fitting between the observed brightness and the spherical harmonic brightnesses. In this work, a 22th order spherical harmonic basis results in a density reconstruction with 540 longitude and 270 latitude bins for a chosen distance (restricted to between 4 and $\approx 10R_{\odot}$, with this range limited by the instrument’s useful field of view). In this work, we use only the reconstructions for a distance of $8R_{\odot}$. Note also that the tomography reconstruction is static - it has no time dependence.
- High-density streamers are narrowed, and a correction for ‘excess’ density, possibly F-corona contamination (Morgan, H. and Habbal, S. R. 2007), is applied according to the method of Morgan and Cook (2020). The narrowing method is applied based on the gradients within the initial tomography density map, with the degree of narrowing controlled by a single parameter. This parameter is adjusted to find an optimal fitting to the observations. The ‘excess density’ is estimated based on an analysis of densities within large low-density regions (coronal holes) between tomography maps made at a range of distances (4 to $8R_{\odot}$), and a consideration of mass flux.

Figure 1a shows the observed coronal polarized brightness. This distribution is very similar to the reconstructed polarized brightness shown in figure 1b. The reconstructed brightness is the result of synthetic observations that use the electron density distribution. The tomography density map resulting from the above steps, is shown in figure 1c. This visualises the distribution of electron density at a distance of $8R_{\odot}$ resulting from the steps described above. Note that this is a static reconstruction, since it gives a non-time-dependent density distribution that is spatially smooth and best satisfies the data.

The distribution of the reconstruction shows a good agreement with the observed, and all the large-scale streamer features are well reconstructed. However, the reconstruction lacks the fine-scale detail of the observed, including a general ‘fuzziness’ of the brightness and temporal changes over timescales of less than a day. To reconstruct fine-scale detail, it is necessary to apply the time-dependent tomography described by Morgan (2021). There is considerable small-scale variation in the nascent slow solar wind (e.g., Alzate et al. 2021, and references within), and the evolution of this variation in the heliospheric wind is an active field of research. For operational forecasting of the ambient solar wind, our immediate problem is to model the large spatial scale and longer-timescale variations, and the static tomography reconstruction is adequate for this purpose.

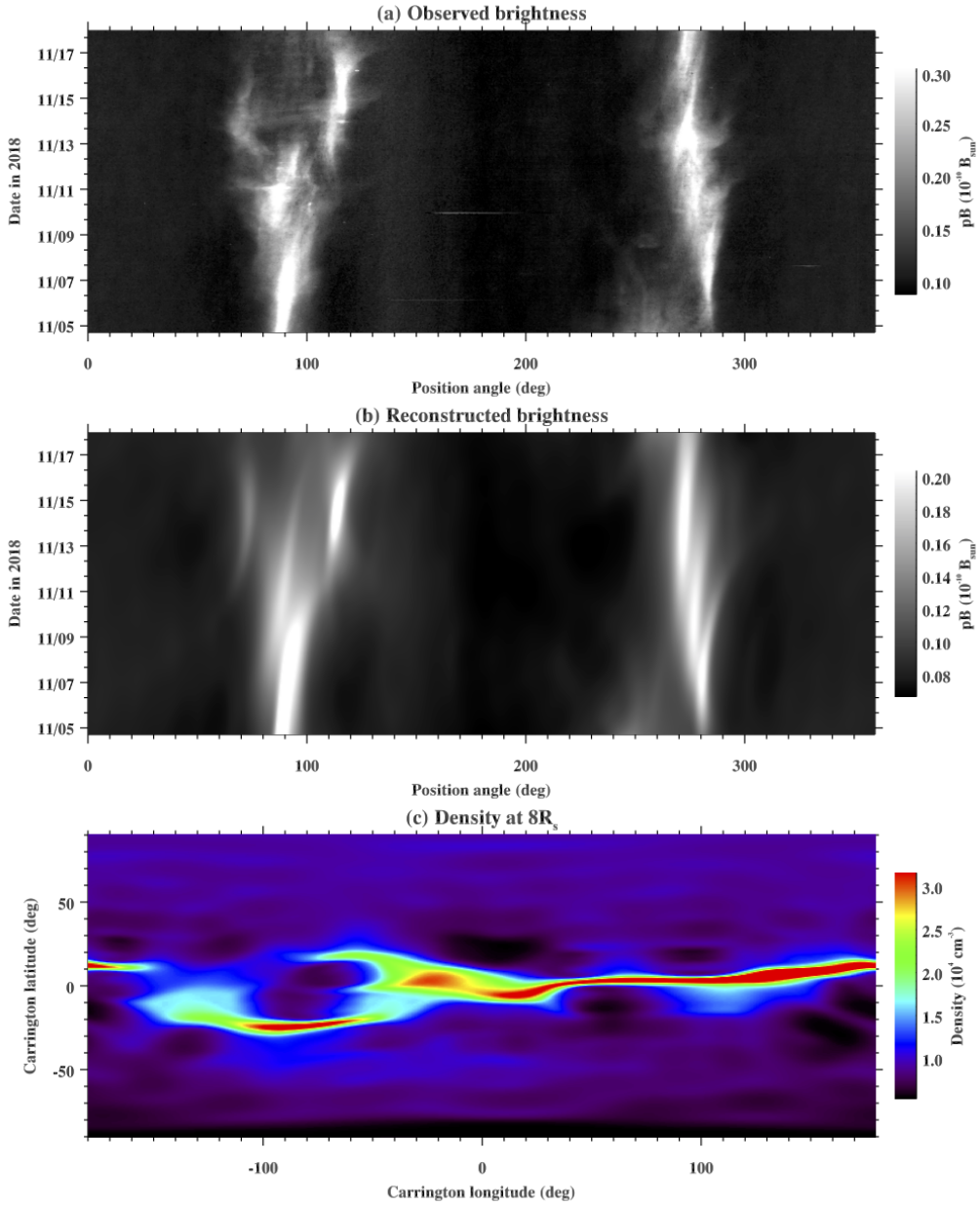


Fig. 1.— (a) The observed coronal polarized brightness at a distance of $8R_{\odot}$, plotted as a function of position angle (measured counter-clockwise from solar north), and time. This is used as input to the tomography method. (b) The reconstructed polarized brightness, or synthetic observations gained from the tomographical density distribution. (c) The electron density at a distance of $8R_{\odot}$, mapped in Carrington longitude and latitude.

2.2. Generating the Inner Boundary Condition

We wish to use the tomography density map as an inner boundary condition to the HUXt model, and to compare the resulting solar wind velocities near Earth with the results of using a MAS-based inner boundary. HUXt allows the user to set the heliocentric distance of the inner boundary. In this work, a distance of $8R_{\odot}$ is used for the tomography-based inner boundary, and $30R_{\odot}$ for the MAS-based inner boundary. For the purpose of solar wind modelling in the Sun-Earth equatorial plane, a slice of density is extracted from the tomography map at Earth’s Carrington latitude at the initiation of the Carrington rotation (this latitude is 4.8° for the 2018 November example). The heliospheric model requires only 128 solar wind velocity values at equally spaced longitudes with increments of $\approx 2.8^{\circ}$. The extracted tomography longitudinal profile is rebinned to this size. Figure 2 shows the density profile at this latitude as a blue curve.

The solar wind model requires a set of radial outward velocities as an inner boundary condition. We adopt a simple linear inverse relationship between densities and velocities, approximately consistent with the general properties of the solar wind as revealed by both *in situ* and remote observations (e.g., Allen et al. 2020; Habbal et al. 1997; Schwenn 2006), given by:

$$V = V_{max} - \left[\left(\frac{n - n_{min}}{n_{max} - n_{min}} \right) (V_{max} - V_{min}) \right], \quad (1)$$

where V and n are the solar wind velocity and electron particle density respectively, n_{max} and n_{min} are the maximum and minimum densities in the equatorial plane respectively, and V_{max} and V_{min} are model parameters specifying the maximum and minimum solar wind velocity at the height of the inner boundary ($8R_{\odot}$). Whereas the density values (n_{max} and n_{min}) are defined by the tomography data at $8R_{\odot}$, the range of the velocity values is unknown. This highlights the need for an optimisation process with the aim of finding optimal values of V_{max} and V_{min} . This optimisation process is described in section 3.1. Figure 2 demonstrates the conversion of the electron density to the solar wind velocity at the inner boundary for the 2018 November (CR2210) example with V_{max} and V_{min} set to their optimal values of 480 and 220 km s^{-1} respectively. Note that these optimal values are found in a following section.

This simple inverse linear relationship of equation 1 is likely oversimplistic compared to the true relationship between density and velocity in the corona, but serves the purpose of providing a proof of concept of a direct relationship for this study. Future efforts will experiment with optimising this empirical relationship, for example, an inverse Sigmoid function or an exponential relationship may better model the likely bimodal slow and fast wind patterns in the nascent solar wind, and may reveal a global model that can provide an optimised model of the solar wind over several years, or a solar cycle. We note that converting the density into an estimate of velocity is a similar approach to that used by magnetic models, where an empirical relationship is required to transform the magnetic field distribution to velocity (e.g. Gonzi et al. 2021).

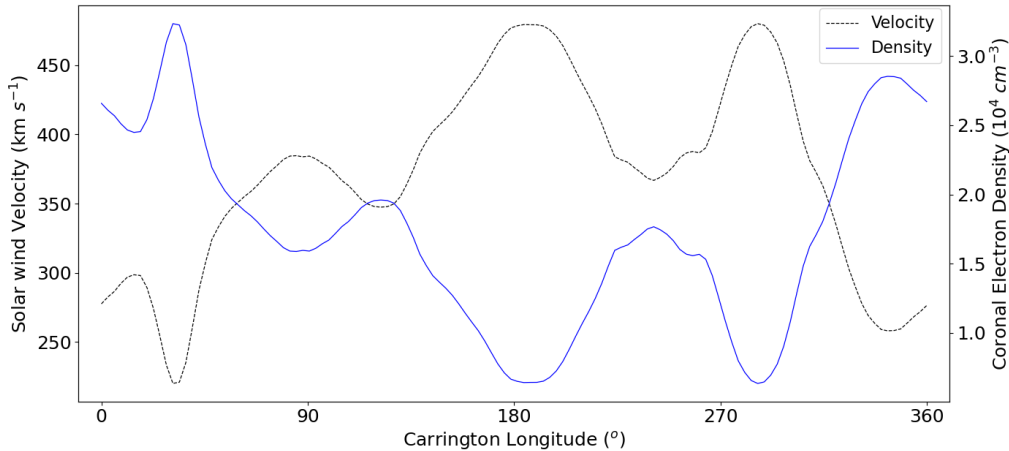


Fig. 2.—: Coronal electron density (blue, right axis) taken from the tomographical map of figure 1c at Earth’s latitude, and solar wind velocity at $8R_{\odot}$ (black, left axis) gained from the density using the simple inverse relationship of equation 1. For this example, $V_{max} = 480 \text{ km s}^{-1}$ and $V_{min} = 220 \text{ km s}^{-1}$.

2.3. Heliospheric Upwind Extrapolation Model

HUXt is an incompressible solar wind model that solves a reduced Burgess equation along 1D vectors of velocities in the radial domain. The ‘upwind’ conditions only allow outward flow and thus forbids any sunward motion of the solar wind. Therefore, considerations for stream interaction are included through adjustments in solar wind speed to uphold the upwind conditions (or at a greater distance in the radial co-ordinate) (Riley and Lionello 2011). For the purposes of forecasting, the results of this model compare well to full 3D MHD models for both predictions of the ambient solar wind and CME events (Hinterreiter et al. 2021; Owens et al. 2020). In this work we use the static tomographical reconstruction and therefore a time-constant boundary condition.

The HUXt model includes a parameter to account for residual solar wind acceleration. Riley and Lionello (2011) used an exponential function to impose a velocity profile that approached its final value asymptotically over a distance range between the lower boundary and $\approx 50R_{\odot}$ (an acceleration parameter of 0.15 which is built in to the HUXt model). In this work, we use this acceleration parameter for both slow and fast wind streams. Investigating this parameter is a central focus of our future work: it is well known that the slow wind reaches its final velocity at a greater distance from the sun compared with that of the fast (e.g., Schwenn 1990).

HUXt uses a five day ‘spin-up’ time. All longitudinal and radial model points are initialised with a value of 400 km s^{-1} . The velocity at the inner boundary condition is rotated through $\approx -66^{\circ}$ (equal to the solar rotation over 5 days), and the solar wind conditions are iteratively propagated outward whilst the boundary condition is rotated forward with time. Therefore, after the five day

‘spin-up’ period, propagated solar wind velocity values have reached distances beyond the orbit of Earth. Following the spin-up period the solar wind velocity conditions are simulated forward in time by 27.27 days (or one rotation). Results that are generated during the spin-up period are discarded from the model output (Owens et al. 2020). For this study, the inner boundary condition is used as a static state which is not altered during the model run.

The evolution of solar wind velocity can be plotted as a function of time at any point in space within the model. In this work, we limit the results to Earth, allowing a direct comparison with *in situ* measurements. We use the reduced 5-min resolution combined satellite network data provided by OMNI. Sporadic short periods of missing solar wind velocity values are linearly interpolated and then binned to form an hourly average with an associated standard deviation. This is then smoothed with a 10-hour moving window average.

2.4. Dynamic Time Warping

Dynamic Time Warping (DTW) is as an effective algorithm to quantify the agreement between two time series and is used here to compare the model and *in situ* solar wind velocities. The DTW algorithm was initially used to aid automated speech recognition and has recently been used in a variety of fields such as economics (Franses and Wiemann 2020), biology (Skutkova et al. 2013), and space weather (Samara et al. 2022; Owens and Nichols 2021).

DTW requires two vectors (1D arrays, A and B) as input. Vectors A and B are not required to be the same length. The Euclidean distance is calculated between every point in set A to every point in set B and is thus assigned a cost function for every possible alignment between the two data sets. This DTW cost or ‘DTW distance’ metric is then minimised to find the optimal alignment between data set A and B (Berndt and Clifford 1994). Effectively, DTW is non-linearly stretching and compressing each data set by connecting like for like structures between the sets. More efficient versions of this algorithm have been generated for reduced computational expense such as the Python FastDTW algorithm package used in this study (See: Salvador and Chan 2004).

The requirements of the DTW algorithm is as follows:

- The two sets are ordered in time.
- Both sets start and end at the same time, or A_0 is anchored to B_0 , and A_{n-1} is anchored to B_{m-1} , where n and m are the number of elements in A and B respectively.
- Every element in data set A will be matched with at least one corresponding data point from data set B , and vice versa.
- The optimum path must not ‘cross’ between elements (for example, if A_i is paired to B_j , then A_{i+1} or later cannot be paired with B_{j-1} or earlier).

A metric used in this study in order to quantify the DTW distance is the Sequence Similarity Factor (SSF). SSF, as defined by Samara et al. (2022), is described in eq 2:

$$SSF = \frac{DTW_{Dist}(O, M)}{DTW_{Dist}(O, \bar{O})} \quad (2)$$

Where M represents the modelled solar wind velocity and \bar{O} represents the average magnitude of the observed *in situ* data (O). SSF allows a direct comparison of the modelled data to that of the averaged *in situ* data and provides a surrogate score of the model. For context, if SSF is > 1 , the predicted solar wind velocities are worse than that of a constant mean observed solar wind value across the full time period of the prediction. If $SSF = 0$, a perfect prediction has been made and the modelled data matches the *in situ* data exactly.

3. Results

3.1. Velocity Optimisation using Dynamic Time Warping

This section describes and implements a simple method to derive optimised values of both the V_{min} and V_{max} terms, and shows how this approach yields a far improved agreement between the model and measured solar wind velocities at Earth, as well as time of arrival of fast solar wind streams.

Figure 3 demonstrates the effect of using arbitrary (and inaccurate) V_{max} and V_{min} velocity terms on the solar wind model values at Earth. V_{max} and V_{min} parameters are set at 600 km s^{-1} and 250 km s^{-1} (shown in figure 3a) and 380 km s^{-1} and 110 km s^{-1} (shown in figure 3b). This figure also visualises the DTW connections between the model and OMNI measurements along the optimum DTW path (shown in red) with the overall DTW distance being visualised by the sum of the length of the red lines. Both overestimation and underestimation of the velocity parameters will cause inaccurate predictions of the solar wind at Earth and thus give a larger DTW path distance compared to a model run with optimised or ‘best fit’ velocity parameters. For example, the magnitude of the DTW path distance metrics for the model runs seen in figure 3 a) and 3 b) are 6.03×10^4 (SSF value of 1.34) and 7.66×10^4 (SSF value of 1.71) respectively. Therefore, both model runs shown in figure 3 provide a greater DTW distance compared to a constant average observed velocity across the full Carrington rotation. In order to obtain velocity values that give an optimal fit (or lowest DTW distance) between the model and *in situ* data, the efficiency of the HUXt model is exploited in an exhaustive search method. The tomography/HUXt model is run repeatedly with incrementally changing V_{max} and V_{min} terms, and the total DTW distance is recorded for each run.

Figure 4a shows the relationship of optimal DTW path distance between the *in situ* and Tomography/HUXt model solar wind velocity at 1AU with incrementally changing velocity terms in equation 1. The velocity ranges used in this study are $50 - 350 \text{ km s}^{-1}$ and $350 - 650 \text{ km s}^{-1}$ for

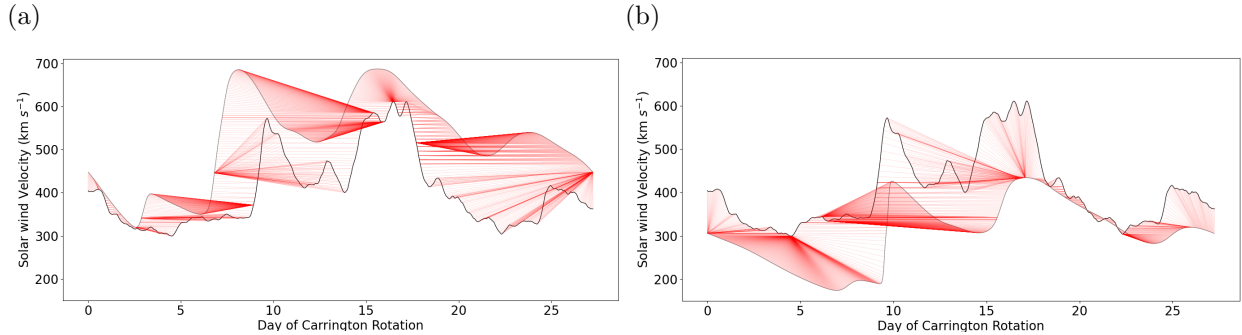


Fig. 3.—: DTW optimal path (red) between *in situ* data and two Tomography/HUXt model runs for CR2210 with a) overestimated V_{max} and V_{min} terms of 600 and 250 km s^{-1} respectively, and b) underestimated V_{max} and V_{min} terms of 380 and 110 km s^{-1} respectively.

V_{min} and V_{max} respectively in order to account for a wide velocity range for each parameter while also constraining each parameter to values that are consistent with physical solar wind velocities. We use 30 increments between these extremes (so $30 \times 30 = 900$ model evaluations). Figure 4a shows a minimum optimal DTW path distance for the tomography derived inner boundary condition corresponding to velocity magnitudes of 220 and 480 km s^{-1} for V_{min} and V_{max} respectively. This is represented by the white cross in figure 4a. These values are lower than observed at Earth due to the HUXt heliospheric model incorporating an acceleration parameter. A comparison between smoothed OMNI satellite data and the HUXt output with the optimal V_{min} and V_{max} is shown in figure 5a, and demonstrates a very strong correlation between the OMNI data and the output of the tomography/HUXt model (for statistical analysis see Table 1). The time of arrival of the faster solar wind streams agree to ± 1 day with the velocities agreeing with $\pm 20 \text{ km s}^{-1}$.

In order for a fair comparison between a tomography and MAS based inner boundary condition (see section 3.2), the MAS inner boundary condition requires a similar exhaustive optimisation process to be applied. This optimisation process effectively scales the initial MAS inner boundary condition between two values (VM_{min} and VM_{max}), with the aim of minimising the DTW path distance between the modelled and *in situ* data. During the optimisation process and for following comparisons, the MAS inner boundary height was set at $30R_{\odot}$. The results of this optimisation can be seen in figure 4b, with the minimum DTW path distance corresponding to VM_{min} and VM_{max} values of 290 and 580 km s^{-1} respectively.

Further details of the agreement of model and observation in the context of a DTW analysis are shown in figure 5. Figure 5a visualises the DTW optimal alignment via the red lines. Figure 5b shows that the DTW path of the optimal alignment rarely deviates over two days from the ‘ideal’ path which represents a near perfect agreement between model and *in situ* data shown in grey. The largest disagreement is seen at 18-24 days, which is seen in both the longer red lines between data points in figure 5a and by the biggest dispersion between the DTW optimum path and the ideal path seen in figure 5b. This is due to a model overestimation of speed during this

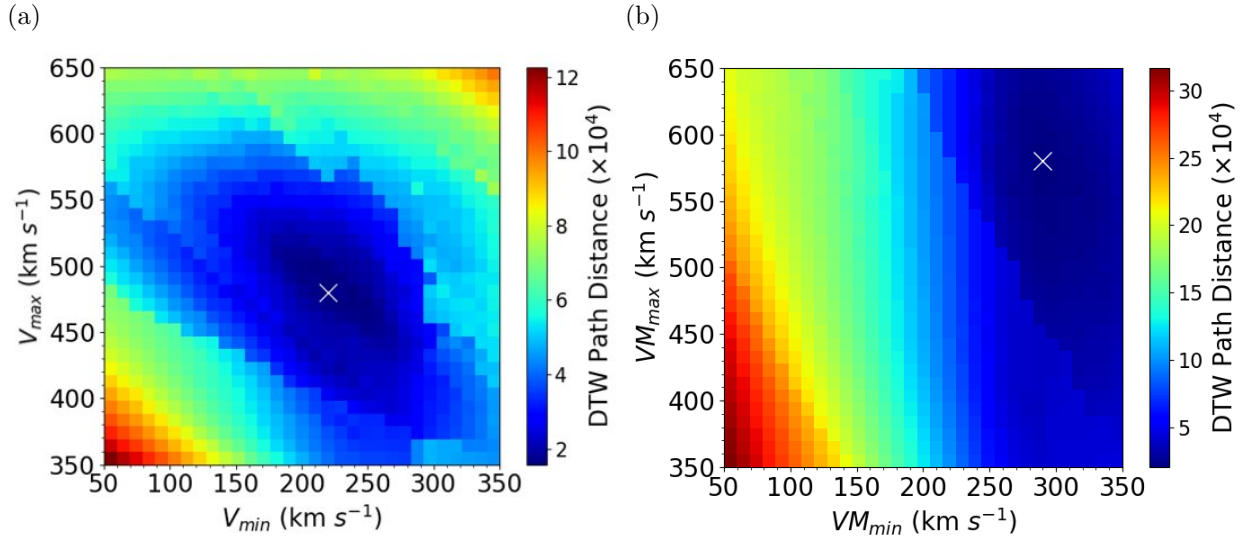


Fig. 4.—: (a) Contour plot of DTW path lengths with varying magnitude of the V_{max} and V_{min} terms for the tomography derived inner boundary condition. The minimum DTW path distance is marked by a white cross, and this point gives the optimal values of V_{max} and V_{min} of 480 and 220 km s^{-1} respectively. (b) DTW path lengths as a function of varying scale parameters for the MAS-derived inner boundary condition with the white cross showing the optimum VM_{min} and VM_{max} parameters of 280 and 580 km s^{-1} respectively.

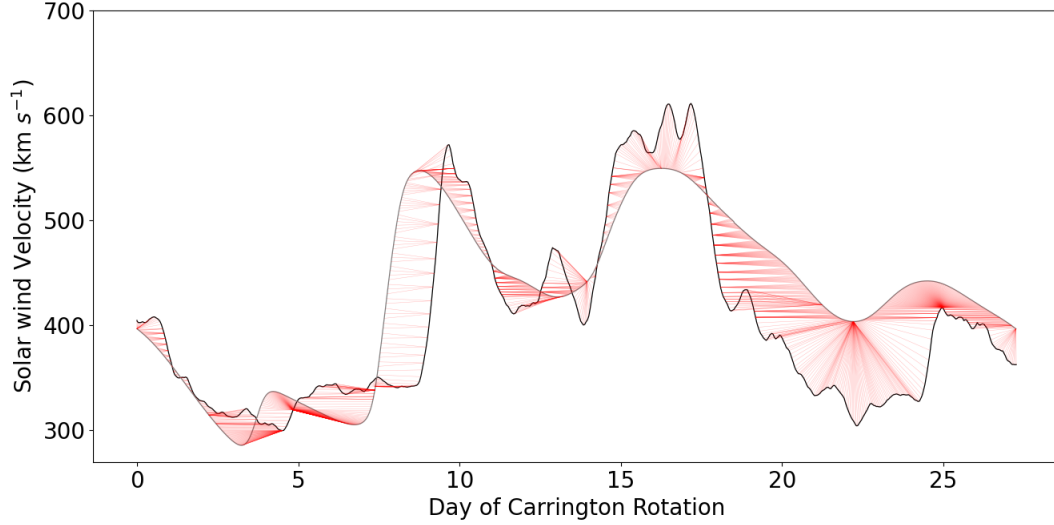
period. The histograms demonstrate the differences in time of arrival and the magnitude of solar wind velocity between the modelled and observational data along the optimum path. Figure 5c shows that there is a bias towards negative values. This suggests the model is predicting a later time of arrival with a mean $\Delta T_{(insitu-model)}$ of -0.45 days, and a standard deviation of 1.16 days. Figure 5d is also biased towards negative values, suggesting velocity overestimation by the model. The mean $\Delta V_{(insitu-model)}$ is -3.64 km s^{-1} with a standard deviation of 19.79 km s^{-1} .

3.2. Validation of Model Output

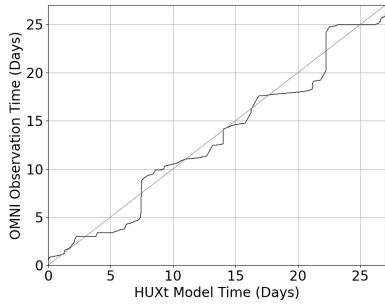
Figure 6 shows a comparison of the CR2210 tomography/HUXt velocity output (Blue) with OMNI *in situ* measurements (Black) at 1AU and MAS/HUXt velocity output (Orange). The tomography based inner boundary parameters V_{min} and V_{max} set at 220 and 480 km s^{-1} respectively. The MAS inner boundary condition has scale parameters of VM_{min} and VM_{max} of 290 and 580 km s^{-1} as described in section 3.1.

From figure 6, both models have similar profiles, and the main changes between slow and fast wind tend to agree. The first small peak (shown in the tomography data 2018 October 29-31) is not present in the MAS data. The solar wind velocity between the second (2018 November

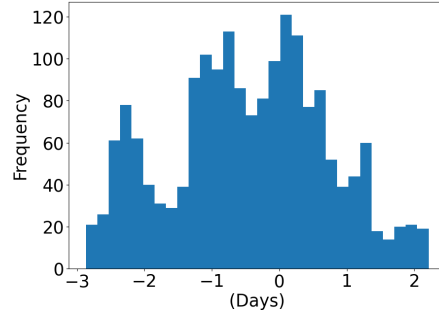
(a)



(b)



(c)



(d)

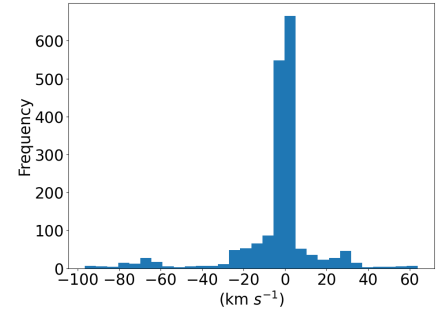


Fig. 5.—: Further analysis of the optimal DTW path. (a) Comparison of modelled solar wind velocities at Earth (grey) with *in situ* data (black) and DTW optimised path (red) (b) Alignment of the modelled and *in situ* data along the optimised DTW path with respect to time. (c) Difference in time between observation and modelled data of aligned points along optimal DTW path ($\Delta T_{(insitu-model)}$) (d) Velocity difference between observation and modelled data of aligned points along optimal DTW path ($\Delta V_{(insitu-model)}$).

2-5) and third peak (2018 November 10-14) drops to intermediate velocities ($\approx 440 \text{ km s}^{-1}$) for the tomography-driven model, whilst the MAS model drops to slower velocity ($\approx 350 \text{ km s}^{-1}$). This is significant as the *in situ* data, as shown in black in figure 6, shows an intermediate velocity ($\approx 440 \text{ km s}^{-1}$) of the more undisturbed solar wind in between the two fast peaks (2018 November 7-10). The magnitude of solar wind velocity during this time is better represented by the tomography inner boundary condition model.

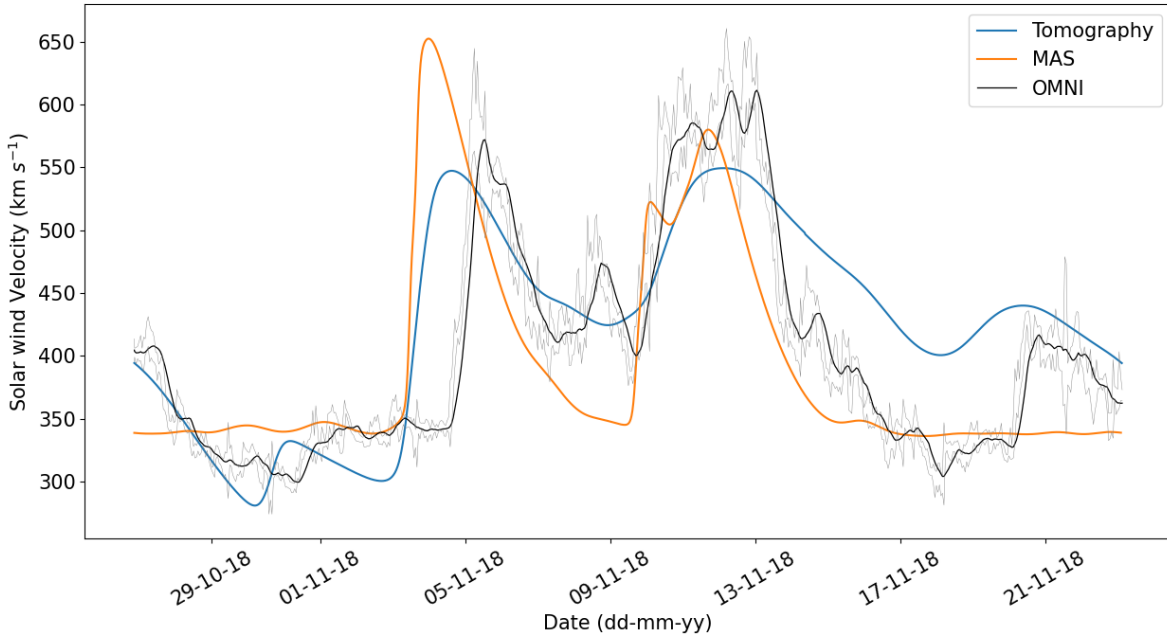


Fig. 6.—: Comparison of optimised tomography/HUXt (blue) and optimised MAS/HUXt (orange) model predictions of the solar wind velocity at Earth with *in situ* data (Black) for CR2210.

Table 1 presents statistical details of the comparison between models. The Pearson correlation coefficient between *in situ* measurements and models is considerably higher for the tomography/HUXt model. The mean absolute error (MAE) of velocities between measurement and MAS/HUXt is approximately 11% higher than that for the tomography/HUXt, while also showing a higher SSF. These results show that the general profile and magnitudes of solar wind velocity is closer to the data using the tomography boundary condition compared to the optimised MAS model. This demonstrates both the potential value of tomographical density maps as an inner boundary condition, and the benefit of searching for an optimised velocity range at the inner boundary. Note that such an optimisation would not be possible without an efficient solar wind model such as HUXt.

Model	MAE (km s^{-1})	Pearson	DTW Path Dist ($\times 10^4$)	SSF
MAS/HUXt	53.58	0.567	2.11	0.47
Tomography/HUXt	47.90	0.7413	1.80	0.40

Table 1:: Statistical analysis of the comparison between the tomography/HUXt model and the MAS/HUXt model, with *in situ* data.

Both models fail to give the exact time of arrival of various features. For example, the rapid rise from slow to fast wind observed on November 4 arrives approximately one day early in both models. The start of the decrease from fast to slow wind on November 13 comes late in the tomography/HUXt model, and the decrease is less rapid than the observed. The main reasons for these differences are listed and discussed in section 5. Despite the differences, the comparison of tomography/HUXt to *in situ* data is promising - the large-scale features of the measured velocity are present in the predicted velocities, and the timings are reasonable given the initial simple implementation of the inner boundary condition. The model fails to replicate smaller-scale structures on timescales of a day or less. One reason for this are that the tomography densities are inherently smooth - this is an unavoidable result of finding a static tomographical solution which is discussed further in section 5. Other reasons for differences between model and measurements include the reduced physics approach of HUXt and the limited resolution of computational modelling.

3.3. Application to other dates

Here we apply the Tomography/HUXt method to two different periods during solar cycle 24. The model is applied to 2014 May (CR2150, near solar maximum) and 2018 March (CR2202, at the start of the current solar minimum). The tomography maps for these two dates are shown in figure 7. Figures 8a and 8c show the comparison of modelled solar wind velocity at Earth and *in situ* data for CR2202 and CR2150 respectfully, with optimised velocity parameters which are gained from the contour plots seen in figure 8b and 8d.

For CR2202, Figure 8b demonstrates a minimum optimal DTW path distance at a V_{max} value of 440 km s^{-1} and a V_{min} value of 230 km s^{-1} . For this period the model and observation data agree well. However, one disparity is present between 2018 March 29 -2018 April 4, where the *in situ* data shows a region of higher solar wind velocity which is not present in the modelled data. The mean velocity difference between *in situ* and modelled data along the optimal DTW warped path is 0.49 km s^{-1} . The time domain also shows an acceptable agreement, with a mean time difference of 1.12 days.

CR2150 spans an active period close to the height of solar maximum. Figure 8c shows a significant fast solar wind stream at 2014 May 22-25 which is seen in both model and measurement. However, there is a large discrepancy between a peak seen in the model at 2014 May 14-16 and one seen in measurement 3 days earlier. Figure 8d demonstrates a minimum optimal DTW path distance at 400 and 240 km s^{-1} for V_{max} and V_{min} respectively. The velocity difference has a mean value of -0.9 km s^{-1} . These values are close to the previous case studies. However the time difference is much greater in comparison to previous Carrington rotations with a mean of -1.6 days and a standard deviation of 2.3 days. Such a deteriorated agreement is likely due to the increased solar activity during this time, which both disrupts the tomography process, makes the time-independent static tomography approach less valid, and increases the chance of CMEs in the *in situ* measurements.

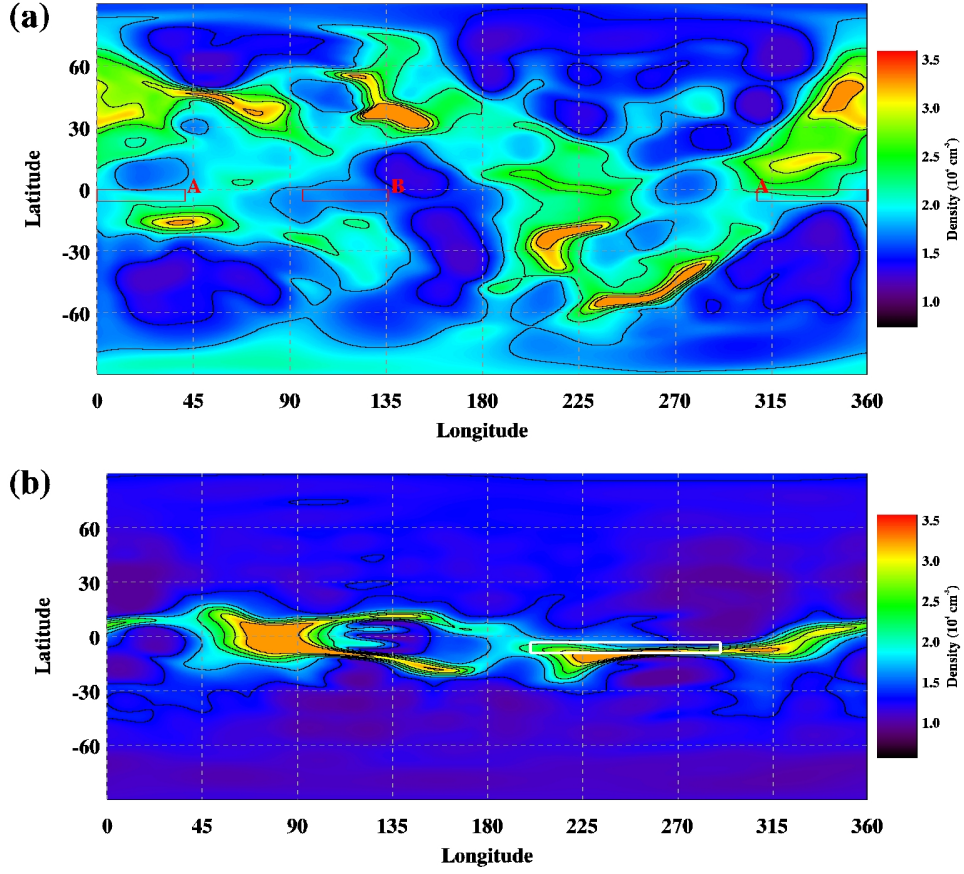


Fig. 7.—: Electron density as estimated using coronal tomography at a distance of $8R_{\odot}$, for Carrington rotations (a) 2150.5, and (b) 2202.5. The red boxes labelled A and B in (a), and the white box in (b), are relevant for the ensemble results of section 4.

Table 2 shows a statistical comparison between both optimised tomography/HUXt and MAS/HUXt models with *in situ* data for CR2150 and CR2202. For CR2150, the tomography/HUXt model combination yields a lower MAE (38.44 km s^{-1}) compared to the MAS/HUXt model (40.12 km s^{-1}). The MAE for CR2202 offers a significant 32% reduction for the tomography/HUXt model (39.31 km s^{-1}), compared to that of the MAS/HUXt model (57.93 km s^{-1}). For both periods, the tomography/HUXt model shows a smaller DTW path distance and a smaller SSF than MAS/HUXt model.

The model solar wind speeds for Carrington rotations 2150 and 2202 show a more gradual transition between high and low solar wind velocities than is seen in the observational data. This is likely due to the smoothness of the density given by the tomography, and the upwind dependence of HUXt. The significant velocity overestimation of $\approx 75\text{-}100 \text{ km s}^{-1}$ seen between 2014 May 27-29 (figure 8c) could be due to the upwind dependence of HUXt, or due to slow wind from equatorial coronal holes. Parker solar probe (PSP) has detected low density - low velocity solar wind structures

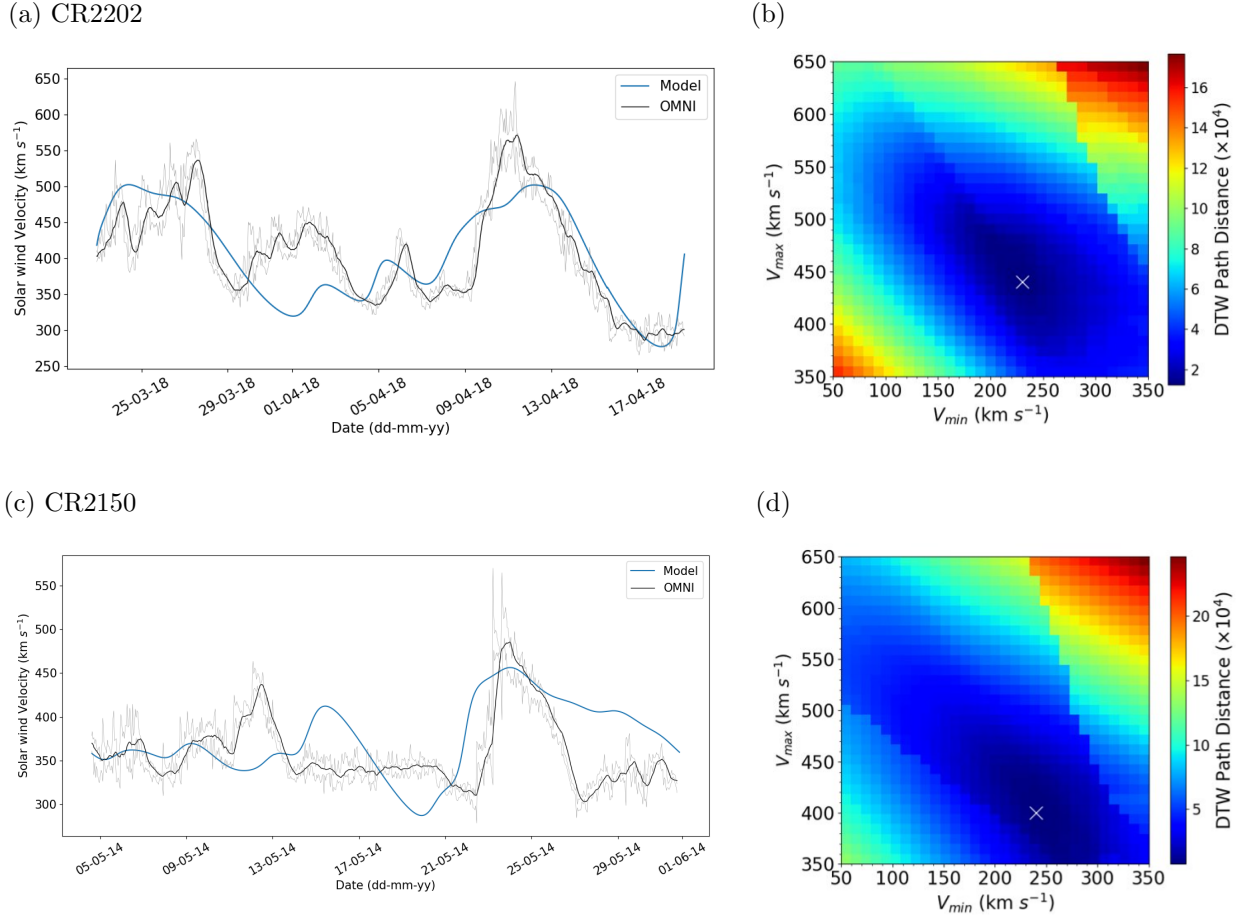


Fig. 8.—: (a) Comparison of model and OMNI solar wind velocities for CR 2202 for the optimal fit in terms of minimum DTW path distance (marked by white cross in figure 8b), with V_{min} and V_{max} set to 230 and 440 km s^{-1} respectively. b) Contour plot showing the DTW path distance as a function of V_{min} and V_{max} for CR 2202. c) Same as (a), but for CR 2150, with V_{min} and V_{max} set to 240 and 400 km s^{-1} respectively (represented by white cross in figure 8d). d) Same as (b), but for CR2150.

at distances close to the sun that are thought to originate from equatorial coronal holes (see: Bale et al. 2019; Kasper et al. 2019). This specific structure of solar wind is in direct contradiction to the simple inverse relationship of equation 1, which assumes a consistent low density - high velocity relationship. This will result in an overestimation of solar wind velocities at the inner boundary and therefore at Earth. A low density - low velocity structure could well be the explanation of the velocity overestimation of 2014 May 27-29 as this region maps back to approximately 150° longitude which is a section in between two coronal holes (see figure 7 a). However, this is an area with obvious key implications for solar wind forecasting that demands further research.

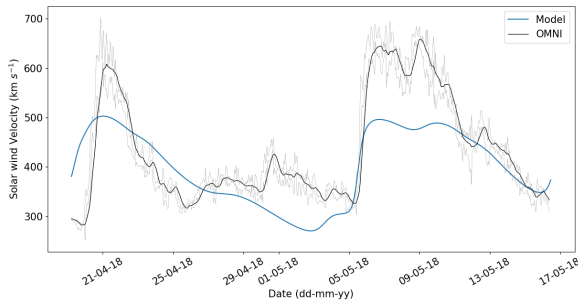
CR	IB	V_{max} (km s^{-1})	V_{min} (km s^{-1})	ΔT (Days)	ΔV (km s^{-1})	MAE (km s^{-1})	DTW Dist ($\times 10^4$)	SSF
2150	Tom	400	240	-1.57 ± 2.31	-0.80 ± 9.83	38.44	0.79	0.42
2150	MAS	390	270	3.61 ± 2.19	0.78 ± 16.10	40.12	1.78	0.95
2202	Tom	440	230	1.12 ± 1.69	0.50 ± 14.92	39.31	1.25	0.34
2202	MAS	420	290	2.98 ± 3.21	-3.34 ± 28.09	57.93	2.39	0.66

Table 2:: Statistics of HUXt model run with both tomography and MAS inner boundaries, with the type of inner boundary indicated by the IB column. The CR column gives the Carrington rotation number, the V_{max} column gives the tomography V_{max} and the MAS VM_{max} parameters, and the V_{min} column gives the tomography V_{min} and the MAS VM_{min} parameters.

3.4. A Persistence Approach

In this section a persistence based approach is adopted in order to attempt to predict solar wind velocities in a realistic operational context. Unlike a traditional persistence model which predicts a near-exact repetition of the observed ambient solar wind conditions for the solar rotation prior (see Owens et al. 2013), in this case the inner boundary condition is updated. The coronal densities (and therefore n_{max} and n_{min} terms in eq. 1) are extracted as described in section 2.2. However, this inner boundary condition will not undergo the exhaustive optimisation process described in section 3.1, but instead use the optimised V_{max} and V_{min} terms unchanged from Carrington rotation prior. For example, figure 9a shows the comparison between *in situ* data and the forecast data for CR2203 with V_{max} and V_{min} values of 440 and 230 km s^{-1} which are the optimised parameters for CR2202. Likewise, figure 9b compares *in situ* data with forecast data for CR2151 with V_{max} and V_{min} of 400 and 240 km s^{-1} (optimised values for CR2150).

(a) CR2203



(b) CR2151

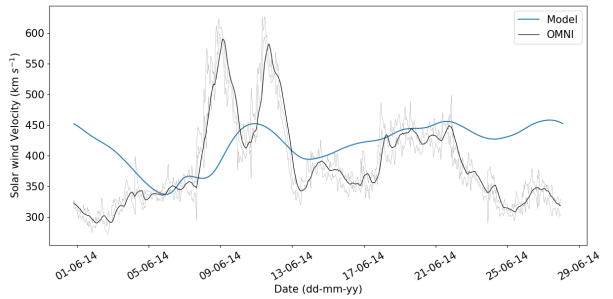


Fig. 9.—: Comparison of predicted solar wind conditions of a) CR2203 (V_{max} and V_{min} of 440 and 230 km s^{-1} respectively) and b) CR2151 (V_{max} and V_{min} of 400 and 240 km s^{-1} respectively). The V_{max} and V_{min} values are that of the optimised velocity terms of the Carrington rotation prior (obtained in section 3.3.)

Figure 9a shows a relatively good agreement with the *in situ* data in terms of time of arrival of the fast solar wind streams (see table 3 for statistical analysis). However, there are disparities in the magnitude of the peaks. For example, in the first peak (seen in the *in situ* data at 2018 April 21-22) the *in situ* data predicts a velocity of $\approx 600 \text{ km s}^{-1}$ whereas, the model predicts a solar wind velocity of $\approx 500 \text{ km s}^{-1}$. The second peak (2018 May 6-11) shows a similar difference. This suggests that the V_{max} term is underestimated. Likewise, the slower more settled solar wind present in between these two peaks (2018 April 25 - 2018 May 5) is underestimated by the model, suggesting that the V_{min} term is also underestimated. Table 3 shows an SSF value of 0.65 for CR2203. This shows that a persistence approach to the tomography based model can yield more accurate results compared to a single mean value.

Figure 9b shows a weaker agreement between the modelled and *in situ* data. The profiles are different, with the *in situ* data demonstrating a double peak between the dates of 2018 June 8-13, whereas the model predicts a single peak around this time. The magnitude of this peak also disagree by $\approx 150 \text{ km s}^{-1}$. This again suggests that the V_{max} term is underestimated. Table 3 shows generally weaker statistics for CR2151 compared to that of CR2203. A SSF value of 1.20 infers that a mean solar wind velocity across the full time period would yield a smaller DTW distance, and potentially better predictions of solar wind velocity compared to a persistence-based approach during this time period. During periods near solar maximum (such as CR2151) we would expect a persistence-based approach to yield worse results. This is due both to the coronal state changing at a significantly faster rate than during solar minimum, and the tomography reconstruction failing to accurately map the true coronal density. Therefore, the inner boundary condition will differ significantly to the physical state of the solar corona. This highlights the need for a time-dependent tomography approach in an operational context.

Car rot.	V_{max} (km s^{-1})	V_{min} (km s^{-1})	MAE (km s^{-1})	Pearson	DTW Path Dist ($\times 10^4$)	SSF
2203	440	230	63.74	0.736	3.77	0.65
2151	400	240	62.067	0.09	4.42	1.20

Table 3:: Statistical analysis of the comparison between the tomography/HUXt model with *in situ* data using optimal velocity parameters gained for the Carrington rotation prior.

Overall, here we show that a persistence model could potentially be used in an operational context as a worst case scenario, without updating the V_{min} and V_{max} parameters. However, the model certainly loses accuracy when deployed in this fashion especially during periods near solar maximum. This stresses the need of either a time-dependent boundary condition, or a more complex, global relationship between coronal electron density and solar wind velocity at a height of $8R_{\odot}$. Both of these issues are the focus of our current efforts.

4. An Ensemble Approach

The high efficiency of the HUXt model allows an ensemble approach to estimate the uncertainty in model outputs based on selected uncertainties at the inner boundary. The tomography density distribution, as shown in figures 1 and 7 show thin elongated structures that tend to lie longitudinally, and can be very narrow in latitude. Therefore, a small error in the distribution given by the tomography method, or small latitudinal deviance of the solar wind during propagation to Earth, can significantly alter the inner boundary condition and the predicted solar wind conditions at Earth. An ensemble approach is a straightforward way of investigating and quantifying the effect small variations in latitude of the extracted tomographical data at the inner boundary can have on the resulting solar wind velocities at Earth. Another uncertainty to which we can apply the ensemble approach is the choice of V_{max} and V_{min} . Here, we use the map of DTW cost function arising from the exhaustive search of V_{max} and V_{min} values to define a range of velocity terms at the inner boundary for 2014 May (CR2150) and 2018 March (CR2202).

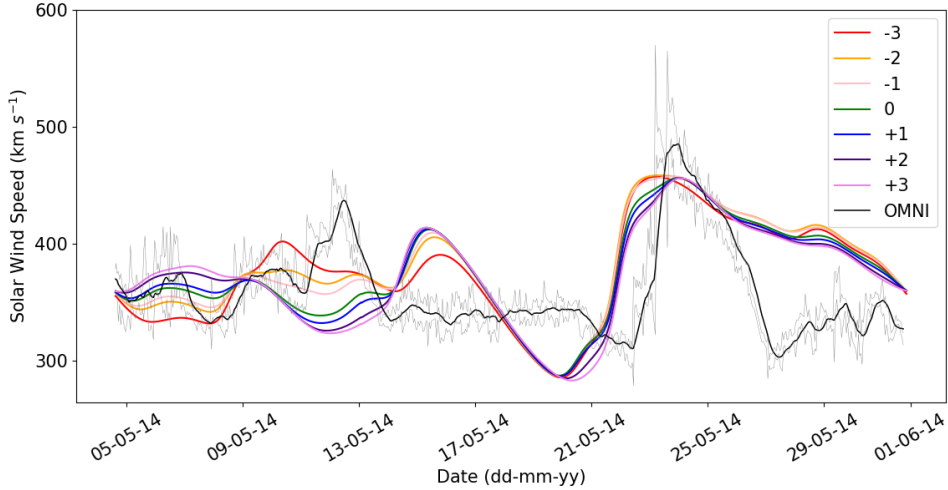
4.1. Latitudinal dependence

Figure 7 shows two density maps that demonstrate two extremes of solar activity. CR2150, as shown in figure 7a, demonstrates a complicated density distribution with many high density streamers positioned at a wide range of latitudes, and which span across the equator. Figure 7b shows a quiet solar corona where the streamer belt is longitudinally aligned near the equator, and a more uniform low electron density at higher latitudes. The main density enhancements are found exclusively in the equatorial region.

A model run was conducted as described in section 3.3 with V_{max} and V_{min} remaining fixed at the optimised values of 400 and 240 km s^{-1} for CR2150 and 440 and 230 km s^{-1} for CR2202. We adjust the inner boundary velocity profile by extracting densities from the tomography map with $\pm 3^\circ$ of the latitude of Earth with 1° increments. This range of latitudes were chosen with the aim of comfortably covering the latitudinal movement of Earth during one full Carrington rotation, and, more importantly, the unknown drift of the solar wind in latitude between the Sun and Earth. Comparisons between the resulting model and measured solar wind conditions at Earth are shown in figure 10. The largest variations in the ensemble velocities during CR2150 (see Figure 10a) are present before 2014 May 13. During this time we find that the relatively small latitude variation of $\pm 3^\circ$ leads to a wide variation in velocity. For example, the largest velocity range is ≈ 50 km s^{-1} observed on 2014 May 10. For the remainder of the period, varying the latitude leads to only a small variation in velocity (≈ 20 km s^{-1}). This can be explained by examining the density map of figure 7a. The solar wind streams at Earth, corresponding to the early part of the period, map back approximately to the region bounded by the red box labelled A in the tomography map. This location was calculated by considering the solar wind speed, the distance from Earth to the tomography map location, and the solar rotation rate. This region spans the boundary between

a high density streamer to the north, and a low density coronal hole to the south. Therefore, the northern latitudes in figure 10a, yield considerably slower solar wind velocities compared to that of southern latitudes during this time. Thus varying the latitude by small values can lead to large changes in the density profile, and therefore the inner boundary velocity.

(a) CR2150



(b) CR2202

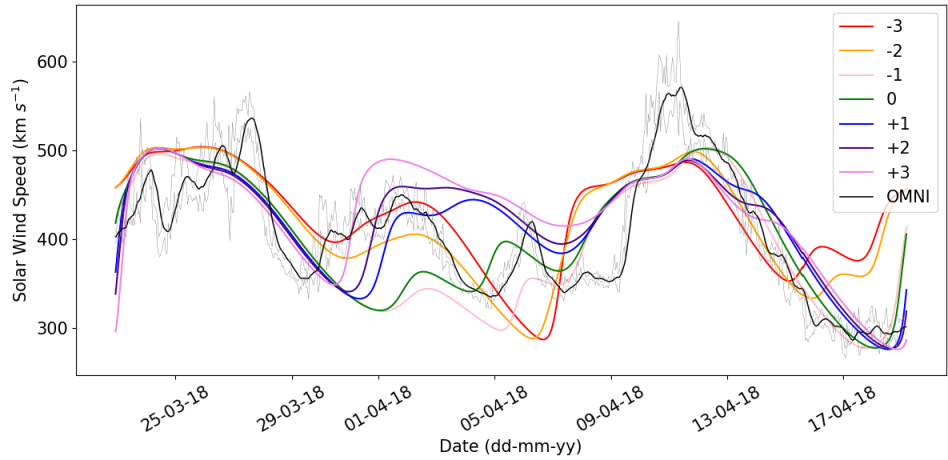


Fig. 10.—: Comparison of *in situ* data with the results of multiple tomography/HUXt model runs for (a) CR2150 and (b) CR2202, with the latitude of the inner boundary condition varied in one degree increments between $\pm 3^\circ$ from the latitude of Earth.

All ensemble model runs fail to match the steep decrease in velocity during 2014 May 25. The coordinates of this decrease near Earth map back to the region bounded by the red box labelled B in

the tomography map. This is a narrow region of low density lying between longitudinally extended regions of higher density to the north and south. Either the tomography map is incorrect in this small area, and that this region should contain a higher density and thus map to slow velocities, or the simplistic inverse linear relationship mapping densities to velocities, as given by equation 1 fails in this region. If the latter, then the relationship should not be linear, and should give highest velocities only for the very lowest density features in the tomography map. Current efforts are focused on the investigation of an improved relationship between coronal electron density and solar wind velocity at $8R_{\odot}$.

All of the ensemble members consistently predict a higher velocity peak at a date of 2014 May 14-16. This feature is not seen on these dates in the *in situ* data. This peak maps back to the small low density feature at Carrington longitude 270° as seen in the equatorial region of the tomography map seen in figure 7a. We note that the density of this feature is low, but not at the minimum densities estimated for coronal holes seen in this map and others. Conversely, the peak at intermediate velocities seen in the data around 2014 May 12 is not present on this date in any of the model runs. This feature maps back to a longitude of around 305° , close to the boundary between the low-density region at 270° . It is likely that the velocity peak seen in all ensemble members (2014 May 14-16) is the same peak seen in the *in situ* data during 2014 May 12. The amplitude of both peaks is comparable. There are several reasons why the model predicted a later time of arrival at Earth for this specific structure, including the modelling limitations of HUXt (e.g. the acceleration parameter), or a defect in the tomography map.

Figure 11 shows how the density of the corona changes in the time of just three Carrington rotations. During CR2149, shown in figure 11a, there is a large and very low density coronal hole spanning the equator and reaching to high latitudes. There is a clearly defined western boundary to this coronal hole at longitude 280° near the equator. By CR2150, as shown in figure 11b, the coronal hole has greatly reduced in size and does not reach the low densities of the previous rotation. Consequently, the western boundary is not clearly defined. The following rotation in figure 11c shows the western streamer encroaching into the region previously occupied by the coronal hole, and the coronal hole limited to southern regions. This rapid change in structure is the best explanation for the differences between the model and *in situ* measurements between dates 2015 May 12 and 18, and shows that a time-dependent inner boundary becomes critical during solar maximum.

The results for CR2202 in figure 10b show that the variability in solar wind prediction is largest between 2018 April 1 to 8, where the model velocities vary by more than 100 km s^{-1} . This region maps back to the white boxed region in figure 7b. This region spans the northern boundary of a high-density streamer, thus small variations in latitude lead to large variations in density and velocity. This result shows that even during quiet periods, large uncertainties can arise from small deviations in latitude. This is a significant problem for solar wind forecasting, particularly considering that the high-density streamer belt may actually be narrower than that reconstructed using tomography. The measured fast wind peak during 2018 April 11 reaches speeds of almost

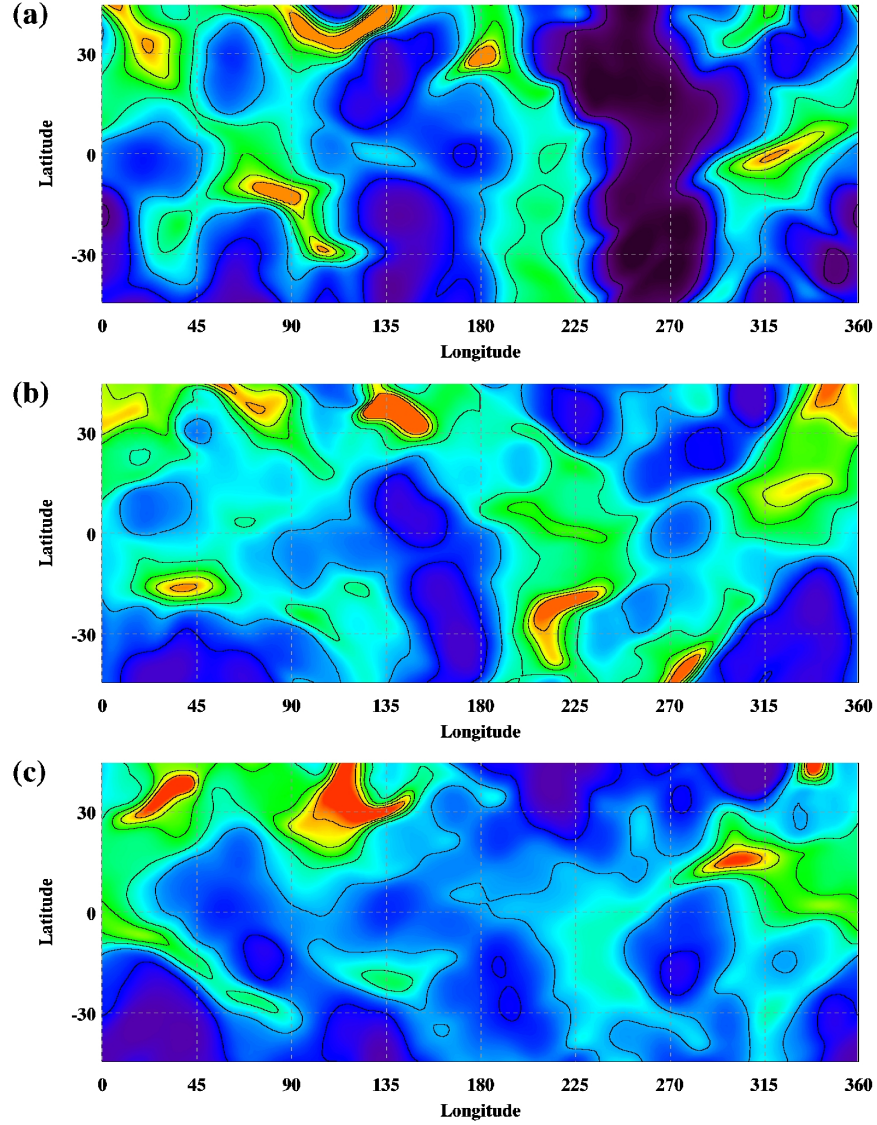


Fig. 11.—: The rapidly changing density of the corona between (a) CR2149, (b) CR2150, and (c) CR2151.

600 km s^{-1} . The models over all latitudes consistently underestimate this peak. This feature maps back to the low density equatorial region near Carrington longitude 145° . This is likely due to the tomography map overestimating the density at this point, or a flaw in the oversimplistic relationship between density and velocity, or a combination of both.

4.2. Velocity dependence

Figure 12 shows the DTW path distance as a function of V_{max} and V_{min} , used to select the optimal parameters. In order to create a velocity-based ensemble, we wish to identify a region within this parameter space where the DTW distance is lower than a set threshold.

Figure 12 shows that there is a selection of velocity values that give an acceptable fit for *in situ* data, defined as $SSF \leq 0.95$. This range of velocity magnitudes defines an uncertainty which is incorporated into the ensemble. The velocity terms for each ensemble member are randomly generated from a normal distribution, with a mean set at the optimal velocity parameters, and a range within three standard deviations of the values that yield a SSF of 0.95 or lower. These regions are highlighted by the white contour in figure 12. For example, CR2150 has mean (optimal) values of 400 and 240 km s^{-1} and a standard deviation of 20 km s^{-1} for V_{max} and V_{min} respectively. For CR2202, mean velocity values are 440 and 230 km s^{-1} with a standard deviation of 30 km s^{-1} . Care was taken in order to ensure V_{max} term was greater than the V_{min} term for every ensemble member.

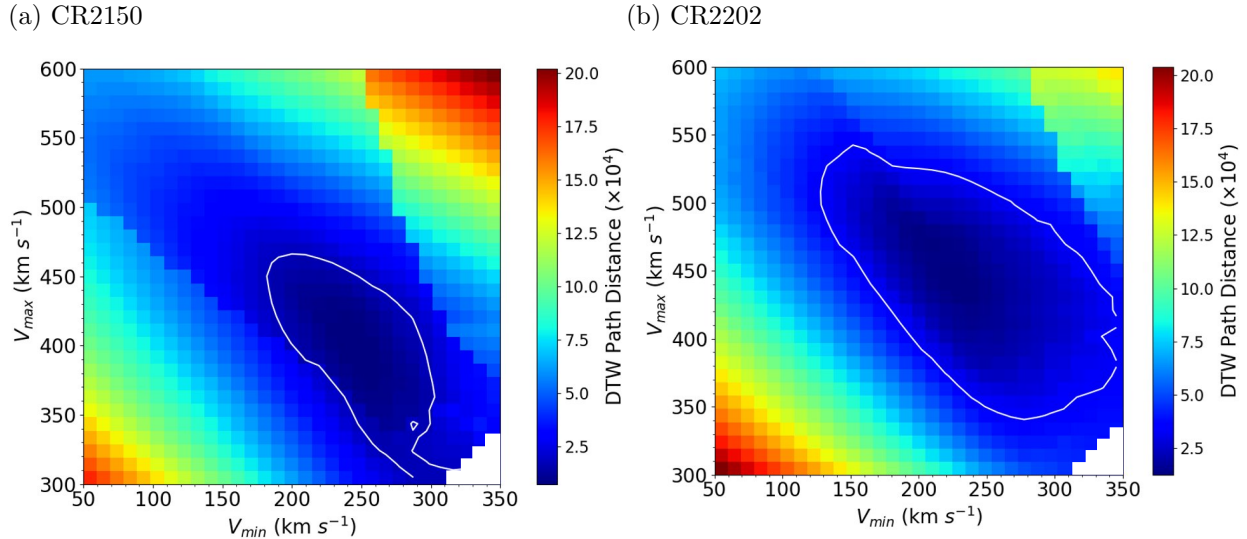
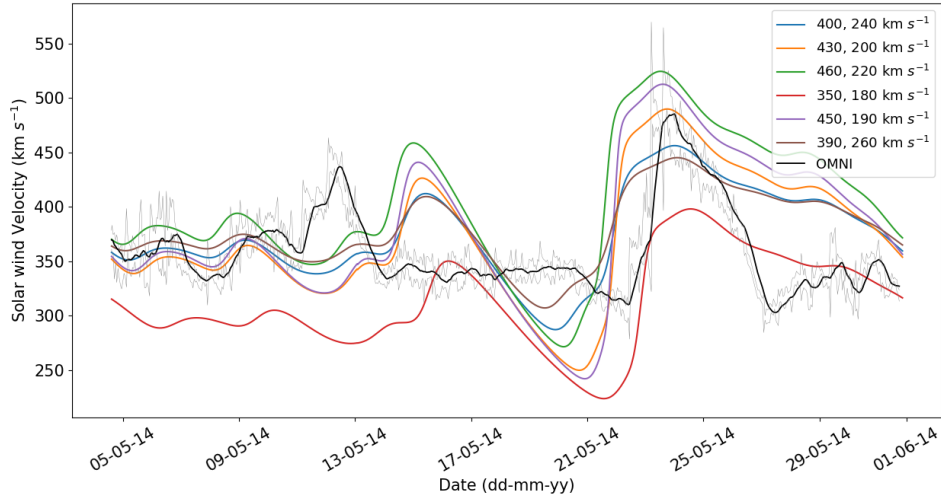


Fig. 12.—: Contour plots of the DTW path distance as a function of minimum and maximum inner boundary velocity for Carrington rotations (a) 2150, and (b) 2202. The white contour bounds the area that yields a DTW path distance of under the threshold chosen ($SSF \leq 0.95$) and the white pixels in the lower right corner represent invalid model parameters where $V_{min} > V_{max}$. Note that the V_{max} range is altered to 300-600 km s^{-1} in this plot.

Figure 13 compares *in situ* data with seven tomography/HUXt outputs each with a different combination of V_{max} and V_{min} magnitudes for CR2150 and CR2202. This highlights the sensitivity of the output to the velocity range. An underestimated V_{max} value will affect the magnitude of the solar wind peaks predicted at Earth, but will also cause the fast solar wind peak to arrive later.

For example in figure 13a, the model with $V_{max} = 350 \text{ km s}^{-1}$ (red) shows a 2-3 day delay in time of arrival of fast solar wind at 2018 May 26, compared with a model run with $V_{max} = 460 \text{ km s}^{-1}$ (green). Both these terms dictate how rapid the transition between fast and slow solar wind occur.

(a) CR2150



(b) CR2202

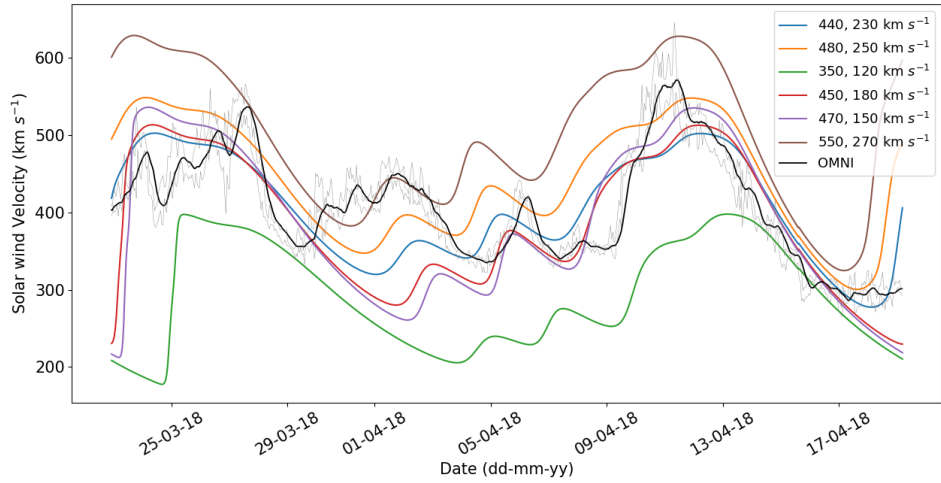


Fig. 13.—: Comparison of *in situ* data with the results of multiple tomography/HUXt model runs for (a) CR2150 and (b) CR2202, with a range of V_{max} and V_{min} combinations.

4.3. Ensemble Results

We create an ensemble with 10,000 unique inner boundary conditions generated with randomly selected pairs of V_{max} and V_{min} taken from a normal distribution around the optimal velocities, and a line of latitude randomly selected between +/- 3 degrees from Earth's latitude at the initiation of the Carrington rotation. Once generated, the 10,000 inner boundary conditions were used for the HUXt model and the results of solar wind velocities at Earth recorded. The results of the ensemble are shown in figure 14. A choice of 10,000 ensemble runs was a compromise between quantifying the sensitivity of the results to the parameter uncertainties with a sensible computation time.

Figure 14a shows a strong correlation between the mean of the ensemble runs (white line) and the optimal HUXt model for the true latitude of Earth (blue line), with a maximum velocity difference of 12 km s^{-1} . The standard deviation of the ensemble around the mean is shown as the dark grey region, and the average standard deviation across the full time series is 20.06 km s^{-1} . The most significant deviations between the *in situ* data and the model data lie at three intervals centered on 2014 May 12, 2014 May 15 (as discussed in section 3.3) and 2014 May 27. The final disparity shows a steep transition between the fast and slow solar wind (seen around 2014 May 28 in the *in situ* data) that is not predicted by any of the 10,000 ensemble model runs.

CR2202, as seen in figure 14b, also demonstrates a good agreement with the *in situ* data with the maximum velocity difference between the mean and the *in situ* data being 79 km s^{-1} . CR2202 shows a greater variability of the ensemble model runs (as shown by the height of both dark grey and light grey regions) compared that of CR2150, with the average standard deviation across the full time-series being 41.7 km s^{-1} . This is approximately double that of CR2150. It would be expected that value is larger than that for CR2150 due to the larger standard deviation entered into the velocity terms (20 km s^{-1} and 30 km s^{-1} for CR2150 and CR2202 respectively).

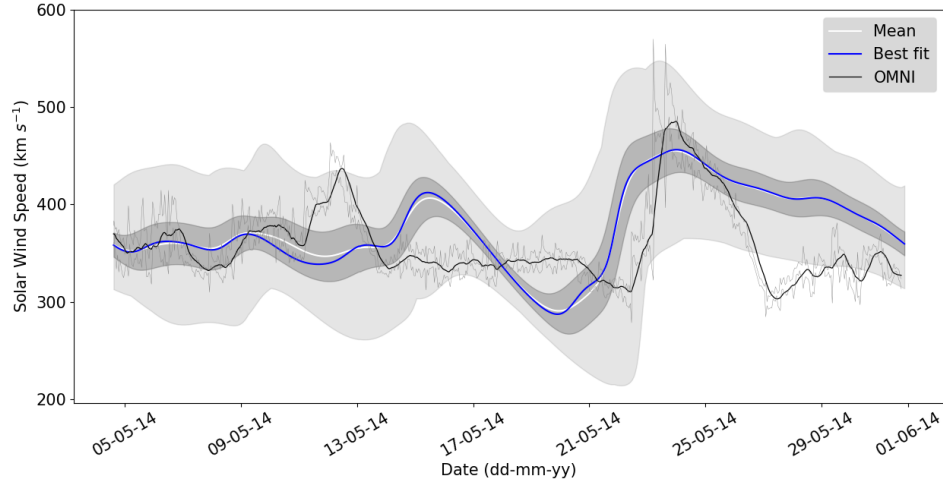
5. Discussion and conclusions

A new inner boundary condition for solar wind heliospheric models is derived from coronal electron density tomography maps. The tomography/HUXt model results give general good agreement with *in situ* data provided by the OMNI satellite network, with a significant increase in the accuracy of solar wind velocity prediction compared to a HUXt model run with a traditional MAS derived inner boundary condition for the time periods used in this study. The time periods investigated in this study were intentionally chosen to demonstrate the model at different stages of the solar activity cycle. Given further development, a future study will explore a larger dataset.

We can identify several aspects of the inner boundary condition and modelling that lead to inaccuracies, and are possible to address with some further work. They are:

- The use of a static tomography reconstruction to represent a dynamic corona. We have recently developed a framework for providing time-dependent tomographical densities, that

(a) CR2150



(b) CR2202

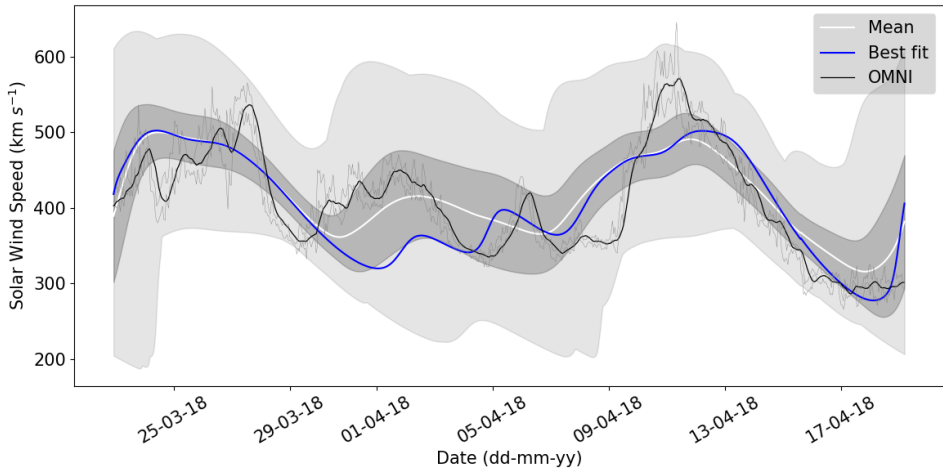


Fig. 14.—: Results of the ensemble for a) CR2150 and b) CR2202 with the mean predicted solar wind velocity at each time step shown as white, the light grey area representing all predicted solar wind velocities, and the darker grey representing one standard deviation from the mean. The non-ensemble model results with the optimal velocity values at the Carrington latitude of Earth is the blue line.

will help address this, although further development is needed (Morgan 2021).

- The overly smooth reconstruction given by tomography compared to the true density. The coronal streamer belt likely consists of very narrow high-density structures (Morgan and Habbal 2010b, 2007b,a) that are highly variable on small temporal (e.g., Alzate et al. 2021)

and spatial scales (Thernisien and Howard 2006; Poirier et al. 2020). Again, developments in tomographical methods and observations can lead to reconstructions that bring us closer to these scales.

- The use of a single, fixed acceleration profile for both fast and slow wind. We are developing our own upwind model that includes both velocities and densities, and includes the acceleration profile as a search parameter. This method uses iteration to improve the fit to *in situ* measurements. Early results are promising, and may provide a constraint on acceleration. Another approach is to use a set of tomographical maps over a range of distances (4 to $10R_{\odot}$) to constrain the early acceleration profile of the slow wind, similar to that shown by Morgan and Cook (2020).
- The simplistic inverse relationship of equation 1. We are investigating the replacement of the simple inverse relationship of equation 1 with a Sigmoid or exponential function, which gives a simple relationship, based on a small number of parameters, to model the transition from slow to fast wind as a function of the density.
- Use of a standard, possibly incorrect, coronal rotation rate. Long time series of tomographical maps can give improved estimates of the variable coronal rotation rate (Edwards et al. 2022; Morgan 2011a,b). Near the equator, the coronal rotation rate may vary by a degree per day or more from the Carrington rate, leading to systematic longitudinal errors in solar wind model results.
- The omission of coronal mass ejections (CME) that may be present in the *in situ* data. This can be addressed to an extent using the current approach for operational forecasting: simple parameters describing a cone model of a CME can be input to HUXt, and the CME carried with the solar wind, giving an estimate of time of arrival at Earth.

A persistence-based approach was made in order to test the operational feasibility of this model. The persistence results showed a large difference in accuracy between periods near solar minimum and maximum. The rate of evolution of the physical corona during solar maximum is such that a persistence approach will break down over timescales of a Carrington rotation. However, during solar minimum, results were more acceptable, yet less accurate than a non-persistence approach. This highlights the need for a time-dependent inner boundary condition, and a more advanced relationship between density and velocity than that given by equation 1.

The efficiency of the HUXt model allows an ensemble framework, which can quantify the uncertainties of the predicted solar wind velocities. The ensembles was based on sampling an appropriate range of latitudes and velocities at the model inner boundary. The ensemble results confirm that both these uncertainties have a significant effect on the model output velocities at Earth. Latitudinally narrow, longitudinally-aligned streamer belt structures can lead to high uncertainties in the output based on small latitudinal uncertainties at the inner boundary. The choice of velocity range at the inner boundary also has a large impact on the model results.

In the context of operational space weather forecasting, this paper shows that the use of a tomography-based inner boundary condition to drive the HUXt model as part of the CORTOM module of the SWEEP project for the UK Met Office is an approach that can offer certain improvements on current systems. Use of multiple models over extended periods will enable an extensive analysis of their relative performance, and the improvements described in this paper will be implemented within SWEEP over the coming years.

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